

CLAIMS:

Having thus described our invention, what we claim as new, and desire to secure by Letters Patent is:

1. In a feedback equalizer device implementing a filter unit performing convolution operations between filter coefficients and one of a plurality of original discrete digital level values for generating a filter output, a multiplier device for multiplying a discrete digital level value with a filter coefficient for said convolution operation, said device comprising:
 - decoder device for receiving a discrete digital level value to be multiplied with said filter coefficient, and implementing logic for generating control signals according to said digital level value;
 - a first sub-multiplication circuit receiving said coefficient and implementing logic for multiplying said filter coefficient by $+1/-1$ or zero (0) in accordance with a first set of control signals and generating a first intermediate multiplication output result therefrom;
 - a second first sub-multiplication circuit simultaneously receiving said number and implementing logic for multiplying said filter coefficient $+1/-1$ or zero (0) in accordance with a second set of control signals and generating a second intermediate output result therefrom;
 - a third sub-multiplication circuit for shifting bits to effect a multiplication of one of said first or second intermediate output result with a discrete digital value different than any of said original plurality of discrete digital level values, and generating a third intermediate result; and,

an accumulator device for adding the results of said third and the other of said first or second intermediate results to obtain a final multiplication result, whereby said final multiplication result of said number with said original discrete digital level value is achieved at a greater speed with less redundancy.

2. The multiplier device as claimed in Claim 1, wherein said decision feedback equalizer is implemented in a communication system for processing signals in accordance with a ATSC (8-VSB) DTV standard, said plurality of original discrete digital level values comprising: $+7/-7$, $+5/-5$, $+3/-3$, and $+1/-1$ and represented as a three (3)-bit code signal.

3. The multiplier device as claimed in Claim 2, wherein said third sub-multiplication circuit shifts bits to effect a multiplication of one of said first or second intermediate output result with a discrete digital value of four (4) or eight (8) in accordance with said control signals.

4. The multiplier device as claimed in Claim 2, wherein said first and second sub-multiplication circuit comprises an inverter circuit.

5. The multiplier device as claimed in Claim 2, wherein said an inverter circuit is implemented as an XOR circuit.

6. The multiplier device as claimed in Claim 2, wherein said accumulator device comprises a carry save adder device for generating sum and carry results.

7. The multiplier device as claimed in Claim 6, wherein said accumulator device further comprises a ripple adder device for adding said sum and carry results.

1 8. The multiplier device as claimed in Claim 7, wherein said ripple adder device receives
2 one or more said control signals for bit correcting bits when a multiplication by -1 is
3 performed according to a first or second control signal step.

1 9. The multiplier device as claimed in Claim 6, further including register for storing a
2 filter output result for use in said convolution operation, said accumulator device further
3 adding a stored filter output result with a final multiplication result of a current iteration.

1 10. The multiplier device as claimed in Claim 2, further including device for encoding an
2 original discrete digital level bit value as a set of bits.

1 11. The multiplier device as claimed in Claim 2, wherein said determined number is an
2 error signal resulting from a recursive decision feedback filter operation.

1 12. Method for performing multiplication in a decision feedback equalizer device
2 implementing a filter unit for performing convolution operations between filter
3 coefficients and one of a plurality of original discrete digital level values, said method
4 comprising:
5

6 a) decoding a discrete digital level value to be multiplied by a filter coefficient, and
7 implementing logic for generating control signals according to said digital level value;
8

9 b) performing two parallel operations, each operation including multiplying said filter
10 coefficient by either $+1/-1$ in accordance with said control signals for generating two
11 intermediate results, and, corresponding operations for multiplying a corresponding
12 intermediate result by $+1$ or zero (0) in accordance with a control signals and generating
13 respective first and second intermediate output results in parallel;

14 c) shifting bits to effect a multiplication of one of said first and second intermediate
15 output result with a discrete digital value different than any of said original plurality of
16 discrete digital level values, and generating a third intermediate result; and,
17
18 d) adding the results of said third and the other of said first or second intermediate results
19 to obtain a final multiplication result, whereby said final multiplication result of said filter
20 coefficient with said original discrete digital level value is achieved at a greater speed
21 with less redundancy.

1 13. The method as claimed in Claim 12, wherein said decision feedback equalizer is
2 implemented in a communication system for processing signals in accordance with a
3 ATSC (8-VSB) DTV standard, said plurality of original discrete digital level values
4 comprising: $+7/-7$, $+5/-5$, $+3/-3$, and $+1/-1$ and represented as a three (3)-bit code signal.

5 14. The method as claimed in Claim 13, wherein said shifting step d) includes the step of
6 shifting bits to effect a multiplication of one of said first or second intermediate output
7 result with a discrete digital value of four (4) or eight (8) in accordance with said control
8 signals.

9 15. The method as claimed in Claim 13, wherein said first multiplication steps circuit
10 comprises performing an inversion of said filter coefficient to be multiplied.

11 16. The method as claimed in Claim 13, wherein steps b) and c) are performed
12 simultaneously.

13 17. The method as claimed in Claim 13, further including the step of storing a filter output
14 result in a register for use during said convolution operation in said filter, said adding step e)

3 including adding said stored filter output result with a final multiplication result of a current
4 iteration to obtain a new filter output value.

1 18. A multiplier device for multiplying one of a set of discrete digital level values with a
2 filter coefficient comprising:

3
4 decoder device for receiving a discrete digital level value to be multiplied and generating
5 control signals according to said digital level value;

6
7 inverter circuit providing two parallel operations, each operation including multiplying said
8 determined number by either +1/-1 in accordance with said control signals for generating two
9 intermediate results;

10
11 multiplier circuit receiving said two intermediate results and providing respective parallel
12 operations for multiplying a corresponding intermediate result of said inverter circuit by +1 or
13 zero (0) in accordance with a control signals and generating respective further intermediate
14 results;

15
16 logic circuit for shifting bits of one further intermediate result to effect a multiplication of one
17 said further intermediate output result with a discrete digital level value different than any of
18 said original plurality of discrete digital level values; and,

19
20 an accumulator device for adding the results of said logic circuit shift multiplication with the
21 other said further intermediate output result to obtain a final multiplication result.

1 19. The multiplier device as claimed in Claim 18, for use in a filter device for performing a
2 convolution operation in an adaptive feedback equalizer implemented in a communication
3 system for processing signals in accordance with a ATSC (8-VSB) DTV standard, wherein
4 said plurality of original discrete digital level values comprising: +7/-7, +5/-5, +3/-3, and

5 +1/-1 and said discrete digital level values different than any of said original plurality of
6 discrete digital level values include four (4) and eight (8) in accordance with said control
7 signals.

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